
Comparative study of stability range of proposed PI controllers for tidal current turbine driving DFIG

Hamed H. H. Aly, M. E. El-Hawary

Department of Electrical and Computer Engineering, Dalhousie University, Halifax, NS, B3H 4R2, Canada

Email address:

hamed.alys@dal.ca (H. H. H. Aly), elhawary@dal.ca (M. E. El-Hawary)

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Abstract: Renewable energy in the power grid system is one of the most important topics in electricity generating now and into the future. The increasing penetration of this type of energy makes it very important for researchers to put the spot on. Tidal current energy is one of the most rapidly growing technologies for generating electric energy. Within that frame, tidal current energy is surging to the fore. The doubly fed induction generator (DFIG) is one of the most commonly used generators associated with tidal current and offshore wind turbines. The aim of the present work is to dedicate control strategies for the DFIG, enabling the turbines to act as an active component in the power system. This paper describes the overall dynamic models of tidal current turbine driving DFIG connected to a single machine infinite bus system and proposed two PI controllers used for improving the power system stability. DFIG is tested for small signal stability analysis. The overall system is verified. The system is tested using different values of controllers coefficients to determine the preferred ranges of values of the controllers coefficients for the system stability. The overall results are discussed and proved the importance of the proposed controllers.

Keywords: Tidal Current Power, Direct Drive Permanent Magnet Synchronous Generator (DDPMSG), Doubly Fed Induction Generator (DFIG), Power System Stability

1. Introduction

In recent years, conventional non-renewable electrical energy production has become an increasing concern due to its high costs, limited resources, and negative influence on global warming from CO₂ emissions. In response to these challenges, scientists have begun to focus their research on renewable energy sources. Renewable energy is generally a clean source of supplying electrical loads, especially in remote and rural areas. Wind energy is one of the most common and rapidly growing renewable energy sources. Wind energy is produced from air motion caused by the uneven heating of the earth's surface by the sun. While wind turbines are associated with negative issues such as noise, visual impacts, erosion, birds and bats being killed, and radio interference, it is still an extremely useful form of energy in rural areas where access to utility transmission facilities is limited. Moreover, the use of wind energy reduces greenhouse gas emissions and positively impacts climate change due to fossil fuel replacement. Worldwide wind capacity is growing fast and may reach up

to 1 million MW by 2050. This means that wind energy integration will become an important factor in the stability of the electric grid. Thus, there is a need for a 'smart' grid that is able to work through any disturbance and supply high quality electric energy to consumers. To date, however, wind power as an energy source is intermittent, challenging to predict, and requires using some form of storage to integrate it into the electric grid. New control techniques and improved forecasting methods are helpful in establishing operating practices that will increase the reliability of wind energy supply [1, 2].

Tidal current energy is the result of the gravitational influence of the moon and the sun on the earth. Due to the rotation of the earth relative to the moon and the sun, two high tides and two low tides are produced in most locations every day (semidiurnal tides), although some locations experience only one high and one low tide daily (diurnal tide). Tides run approximately six hours in one direction and then reverse for another six hours in the opposite direction. There are two tide types: spring tide (the speed of the spring tides varies from 3.5 to 4m/s), which happens when the moon and the sun are on the same line, and neap tide

(the speed of the neap tides varies from 2 to 2.5m/s), which happens when the moon and the sun are at right angles and pull seawater in different directions. Nova Scotia's Bay of Fundy is characterized by high tides that can reach up to 17 meters. The electrical-side layout and modeling approaches used in tidal in-stream systems are similar to those used for wind and offshore wind systems. The speed of water currents is lower than wind speed, while the water density is higher than the air density and as a result wind turbines operate at higher rotational speeds and lower torque than tidal in-stream turbines which operate at lower rotational speed and high torque [1-5].

The easier predictability of the tidal in-stream energy resource makes it easier to integrate in an electric power grid. Recognizing that future ocean energy resources are available far from load centers and in areas with limited grid capacity will result in challenges and technical limitations. With the growing penetration of tidal current energy into the electric power grid system, it is very important to study the impact of tidal current turbines on the stability of the power system grid and to do that we should model the overall system. The model of the ocean energy system consists of three stages. The first stage contains the fluid mechanical process. The second stage consists of the mechanical conversion and depends on the relative motion between bodies. This motion may be mechanical transmission and then using mechanical gears or may be depending on the hydraulic pumps and hydraulic motors. The third stage consists of the electromechanical conversion to the electrical grid [4-8].

DFIG and DDPMSG are the most commonly used generators with tidal current turbines. Different controllers are used for stabilization of DFIG and DDPMSG for both the grid side converter and the generator side converter for offshore wind turbines. Some of these controllers use the generator side converter controller to maintain the rotational speed of the generator at an optimal value, and minimize the core losses; and use the grid side converter controller to maintain the voltage of the DC-link, and control the output reactive power to a certain level. Other controllers use the generator side converter controller for controlling the output active power and reactive power, while using the grid side converter controller for controlling the DC-link voltage and the terminal voltage of the turbine system [3, 9]. The following sections describe the dynamic model of the whole system including the proposed controllers and the state space representation of the whole system.

Nomenclature

V_{tide}	Tidal current speeds.
V_{nt}	Neap tide speed.
V_{st}	Spring tide speed.
C_s	Constant and equals 95 for spring, 45 for neap tide.
P_{ts}	Tidal in-stream power.
ρ	Density of the water (1025 kg/m ³)
A	Cross-sectional area perpendicular to the flow direction.
T_m	Mechanical torque applied to the turbine.

A	Cross-sectional area perpendicular to the flow direction.
C_p	Marine turbine blade design constant in the range of 0.35-0.5.
$\omega_s, \omega_r, \omega_t$	Stator, rotor electrical angular velocities, and turbine speed at hub height upstream the rotor.
T_e	Electrical torque of the generator.
D_s	Shaft stiffness damping.
H_t, H_g	Turbine and generator inertia constants.
K_s	Shaft stiffness coefficient.
\square_t, \square_r	Turbine and generator rotor angles.
β	Tidal turbine pitch angle.
S	Rotor slip.
d, q	Indices for the direct and quadrature axis components.
s, r	Indices of the stator and the rotor.
v, R, i, ψ	Voltage, resistance, current, and flux linkage of the generator.
K_{pt}, K_{lt}	Coefficients for the proportional-integral controller of the pitch controller.
P_g, P_{DC}	Active power of the AC terminal at the grid side converter and DC link power respectively.
v_{Dg}, v_{Qg}	D and Q axis voltages of the grid side converter.
i_{Dg}, i_{Qg}	D and Q axis currents of the grid side converter.
C	Capacitance of the capacitor.
v_{DC}, i_{DC}	Voltage and current of the capacitor.
K_{p1}, K_{p2}, K_{p3}	Proportional controller constants for the generator side converter controller
K_{i1}, K_{i2}, K_{i3}	Integral controller constants for the generator side converter controller.
i_{Dg}, i_{Qg}	D and Q axis grid currents.
v_{Dg}, v_{Qg}	D and Q axis grid voltages.
K_{p4}, K_{p5}, K_{p6}	Proportional controller constants for the grid side converter.
K_{i4}, K_{i5}, K_{i6}	Integral controller constants for the grid side converter.
X_c	Grid side smoothing reactance.
\dot{x}	State variable

2. Tidal Current Model using DFIG

This section reviews the dynamic model of the tidal current turbine system, DFIG, the converter and the proposed controllers.

2.1. The Speed Signal Resource Model

The tidal current speed may be expressed as a function of the spring tide speed, neap tide speed and tides coefficient (Cs). Hence knowing tides coefficient, it is easy to derive a simple and practical model for tidal current speeds as follows [3, 10]:

$$V_{tide} = V_{nt} + \frac{(C_s - 45)(V_{st} - V_{nt})}{95 - 45}$$

2.2. The Rotor Model

The power (P_{ts}) may be found using: $P_{ts} = \frac{1}{2} \rho A (V_{tide})^3$. The turbine harnesses a fraction of this power, hence the power output may be expressed as: $P_t = \frac{1}{2} \rho C_p A (V_{tide})^3$. The power output is proportional to the cube of the velocity. The velocity at the bottom of the channel is lower than at the water column above seabed. The mechanical torque applied to the turbine (T_m) can be expressed as [4-9]:

The shaft system may be represented by a two mass system one for the turbine and the other for the generator as shown:

$$T_m = \frac{0.5\rho\Pi R^2 C_p v_{tide}^3}{\omega_t} \quad (1)$$

$$2H_t \frac{d\omega_t}{dt} = T_t - K_s(\Theta_r - \Theta_t) - D_s(\omega_r - \omega_t) \quad (2)$$

$$2H_g \frac{d\omega_r}{dt} = T_e - K_s(\Theta_r - \Theta_t) - D_s(\omega_r - \omega_t) \quad (3)$$

$$\Theta_{tr} = \Theta_r - \Theta_t \quad (4)$$

$$\frac{d\Theta_{tr}}{dt} = \omega_r - \omega_t \quad (5)$$

There is a ratio for the torsion angles, damping and stiffness that need to be considered when one adds a gear box as all above calculations must be referred to the generator side and calculated as : $a = \frac{\omega_r}{\omega_t}$, $\omega_r^{(t)} = \frac{\omega_r^{(g)}}{a}$, $t = \frac{t}{a}$, $K_s^{(t)} = a^2 K_s^{(g)}$, $D_m^{(t)} = a^2 D_m^{(g)}$. The same model used for the offshore wind is used for tidal in-stream turbines; however, there is a number of differences in the design and operation of marine turbines due to the changes in force loadings, immersion depth, and different stall characteristics. Since the extracted power from the tidal currents is proportional to the area and the cube of the velocity, hence narrow channels is preferred for tidal turbines to extract higher power as the velocity is higher.

2.3. Dynamic Model of DFIG

The DFIG model is developed using a synchronously rotating d-q reference frame with the direct-axis oriented along the stator flux position. The reference frame rotates at the same speed as the stator voltage. The stator and rotor active and reactive power are given by [4-10]:

$$P_s = 3/2(v_{ds} i_{ds} + v_{qs} i_{qs}) \quad , \quad P_r = 3/2(v_{dr} i_{dr} + v_{qr} i_{qr}) \quad (6)$$

$$P_g = P_s + P_r \quad (7)$$

$$Q_s = 3/2(v_{qs} i_{ds} - v_{ds} i_{qs}) \quad , \quad Q_r = 3/2(v_{qr} i_{dr} - v_{dr} i_{qr}) \quad (8)$$

The model of the DFIG can be described as:

$$v_{ds} = -R_s i_{ds} - \omega_s \Psi_{qs} + \frac{d}{dt} \Psi_{ds} \quad (9)$$

$$v_{qs} = -R_s i_{qs} + \omega_s \Psi_{ds} + \frac{d}{dt} \Psi_{qs} \quad (10)$$

$$v_{dr} = -R_r i_{dr} - s \omega_s \Psi_{qr} + \frac{d}{dt} \Psi_{dr} \quad (11)$$

$$v_{qr} = -R_r i_{qr} + s \omega_s \Psi_{dr} + \frac{d}{dt} \Psi_{qr} \quad (12)$$

$$\Psi_{ds} = -L_{ss} i_{ds} - L_m i_{dr} \quad , \quad \Psi_{qs} = -L_{ss} i_{qs} - L_m i_{qr} \quad (13)$$

$$\Psi_{dr} = -L_{rr} i_{dr} - L_m i_{ds} \quad , \quad \Psi_{qr} = -L_{rr} i_{qr} - L_m i_{qs} \quad (14)$$

$$s = (\omega_s - \omega_r) / \omega_s \quad (15)$$

$$\frac{d\omega_r}{dt} = -\omega_s \frac{ds}{dt} \quad (16)$$

Where, $L_{ss} = L_s + L_m$, $L_{rr} = L_r + L_m$, L_s , L_r and L_m are the stator leakage, rotor leakage and mutual inductances, respectively. The previous model may be reduced by neglecting stator transients and is described as follows:

$$v_{ds} = -R_s i_{ds} + X \square i_{qs} + e_d \quad (17)$$

$$v_{qs} = -R_s i_{qs} - X \square i_{ds} + e_q \quad (18)$$

$$\frac{de_d}{dt} = -\frac{1}{T_0} (e_d + (X - X) i_{qs}) + s \omega_s e_q - \omega_s \frac{L_m}{L_{rr}} v_{qr} \quad (19)$$

$$\frac{de_q}{dt} = -\frac{1}{T_0} (e_q - (X - X) i_{ds}) - s \omega_s e_d + \omega_s \frac{L_m}{L_{rr}} v_{dr} \quad (20)$$

The components of the voltage behind the transient (the internal voltage components of the induction generator) are $e_d = -\frac{\omega_s L_m}{L_{rr}} \psi_{qr}$ and $e_q = \frac{\omega_s L_m}{L_{rr}} \psi_{dr}$. The stator reactance $X = \omega_s L_{ss} = X_s + X_m$, and the stator transient reactance $X \square = \omega_s (L_{ss} - L_m^2 / L_{rr}) = X_s + (X_r - X_m) / (X_r + X_m)$. The transient open circuit time constant is $T_0 = L_{rr} / R_r = (L_r + L_m) / R_r$, and the electrical torque is $T_e = (i_{ds} i_{qr} - i_{qs} i_{dr}) X_m / \omega_s$.

2.4. The Pitch Controller Model

The pitch controller is used to adjust the tidal current turbine to achieve a high speed magnitude. This may be represented by a PI controller with a transfer function $K_{pt} + \frac{K_{it}}{s}$ shown in Figure (1).

$$\beta = (K_{pt} + \frac{K_{it}}{s}) \omega_t \quad (21)$$

$$\frac{d\beta}{dt} = K_{pt} \frac{d\omega_t}{dt} + K_{it} \omega_t \quad (22)$$

ence between the grid terminal voltage and the reference terminal voltage required at a certain time, x_6 is a combination of x_5 and direct axis grid current and x_8 is a combination of x_6 and quadrature axis grid current as shown in equations (35-40). Figure (4) shows the grid side converter controller.

$$\dot{x}_5 = v_{DC_ref} - v_{DC} \quad (35)$$

$$\dot{x}_6 = K_{p4}\dot{x}_5 + K_{i4}x_5 - i_{Dg} \quad (36)$$

$$\dot{x}_7 = v_{t_ref} - v_t \quad (37)$$

$$\dot{x}_8 = K_{p6}\dot{x}_7 + K_{i6}x_7 - i_{Qg} \quad (38)$$

$$v_{Dg} = K_{p5}\dot{x}_6 + K_{i5}x_6 + X_c i_{Qg} \quad (39)$$

$$v_{Qg} = K_{p5}\dot{x}_8 + K_{i5}x_8 - X_c i_{Dg} \quad (40)$$

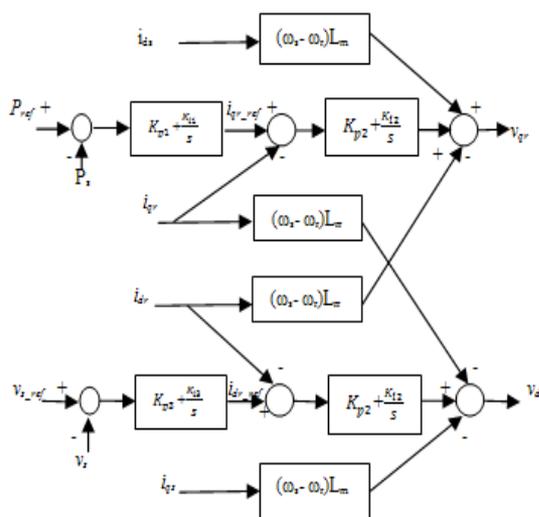


Figure 4. Grid side converter controller

3. State Space Representation and Small Signal Stability Analysis of The System

In this section we describe the state space representation of the whole system and apply the small signal stability analysis of a single machine infinite bus system for tidal current turbine using DFIG. Small signal stability is the ability of the power systems to remain in synchronism under small disturbances. Small signal stability analysis for the power system determines the properties of operation of the system due to small disturbance in the system. This is done by finding the eigenvalues of the system for a small change that may have happened. In this section we perturb each state of the system by a small increment Δ , keeping in mind some assumptions [15]. These assumptions are: $\Delta^2=0$,

$\sin\Delta=0$ and $\cos\Delta=1$. Using these assumptions we can rewrite the state space equations as:

$$\Delta\dot{x} = A\Delta x + B\Delta u$$

$$\Delta x \text{ for DFIG} = [\Delta w_t, \Delta\beta, \Delta v_{DC}, \Delta\Theta_{tr}, \Delta e_d, \Delta e_q, \Delta V_{DC}, \Delta x_1, \Delta x_2, \Delta x_3, \Delta x_4, \Delta x_5, \Delta x_6, \Delta x_7, \Delta x_8]^T$$

The fifteen states of the DFIG are $w_t, \beta, v_{DC}, \Theta_{tr}, e_d, e_q, V_{DC}, x_1, x_2, x_3, x_4, x_5, x_6, x_7$ and x_8 . Equations (2), (3), and (5) are used for the drive train. Equations (19) and (20) are used for the generator. Equations (23), (24), and (25) for the DC link give v_{DC} state. Equations from (26) to (34) are used for the generator side converter controller model and give the states x_1 and x_2 . Equations from (35) to (40) are used for the grid side converter controller.

4. Effect of Changing the Controllers Coefficients Values

As the values of the controllers coefficients change, the stability will change. In this section we will try to change the values of the controllers coefficients independently and try to find the relation between the increasing or decreasing of these coefficients independently and the degree of the stability. Also we will try to rank the importance of these coefficients for the stability analysis.

4.1. DFIG Controllers Coefficient

In this section we try to do some computational work that compares the effects of specific parameters change on stability for DFIG. At the end of this section we discuss the preferred ranges of values of the controllers for the stability of the system. Table (1) gives the eigenvalues of the 15th order model of the whole system using DFIG for different values of the proportional coefficient controller K_{p1} . From table (1) we conclude that the system is asymptotically stable. The eigenvalues related to the voltage states (e_d, e_q) have imaginary parts equal to 50 and -50 and real parts equal to -1 and +1.

Tables (1- 6) show the effect of changing the values of the proportional controllers coefficients for DFIG on stability analysis. The coefficients may be ranked depending on its effects on the stability. The most effective proportional coefficient controller is K_{p2} . This coefficient affects on two modes of states and made a huge change on the locations of these two poles. The six proportional coefficients may be ranked from the most effective to the least effective depending on the change that they made on the eigenvalues compared to the change on their own values as $K_{p2}, K_{p3}, K_{p1}, K_{p4}, K_{p6}, K_{p5}$.

Tables (7- 12) show the effect of changing the values of the integral controllers coefficients for DFIG on stability analysis. The coefficients may be ranked depending on their effect on the stability. The most effective proportional coefficient controller is K_{i3} . The integral coefficients may

be ranked from the most effective to the least effective depending on the changed that they made on the eigenvalues compared to the change on their own values as K_{i3} , K_{i1} , K_{i2} ,

K_{i4} , K_{i5} , K_{i6} . Table (13) shows the range of values for the controllers coefficients for DFIG.

Table 1. Eigenvalues of the DFIG for changing the proportional coefficient value K_{p1}

	σ $K_{p1} = 0.5$	ω	σ $K_{p1} = 0.75$	ω	σ $K_{p1} = 1$	ω	σ $K_{p1} = 1.25$	ω
λ_1	-10	-	-10	-	-10	-	-10	-
λ_2	-1542.9	-	-1542.9	-	-1542.9	-	-1542.9	-
λ_3	-1	+j50	-1	+j50	-1	+j50	-1	+j50
λ_4	-1	-j50	-1	-j50	-1	-j50	-1	-j50
λ_5	-2	+j3	-2	+j3	-2	+j3	-2	+j3
λ_6	-2	-j3	-2	-j3	-2	-j3	-2	-j3
λ_7	-1444	-	-1444	-	-1444	-	-1444	-
λ_8	-200	-	-133	-	-100	-	-80	-
λ_9	-27	-	-27	-	-27	-	-27	-
λ_{10}	-175	-	-175	-	-175	-	-175	-
λ_{11}	-27	-	-27	-	-27	-	-27	-
λ_{12}	-10	-	-10	-	-10	-	-10	-
λ_{13}	-8	-	-8	-	-8	-	-8	-
λ_{14}	-10	-	-10	-	-10	-	-10	-
λ_{15}	-27	-	-27	-	-27	-	-27	-

Table 2. Eigenvalues of the DFIG for changing the proportional coefficient value K_{p2}

	σ $K_{p2} = 0.05$	ω	σ $K_{p2} = 0.15$	ω	σ $K_{p2} = 0.3$	ω	σ $K_{p2} = 0.45$	Ω
λ_1	-10	-	-10	-	-10	-	-10	-
λ_2	-1542.9	-	-1542.9	-	-1542.9	-	-1542.9	-
λ_3	-1	+j50	-1	+j50	-1	+j50	-1	+j50
λ_4	-1	-j50	-1	-j50	-1	-j50	-1	-j50
λ_5	-2	+j3	-2	+j3	-2	+j3	-2	+j3
λ_6	-2	-j3	-2	-j3	-2	-j3	-2	-j3
λ_7	-1444	-	-1444	-	-1444	-	-1444	-
λ_8	-100	-	-100	-	-100	-	-100	-
λ_9	-160	-	-53	-	-27	-	-18	-
λ_{10}	-175	-	-175	-	-175	-	-175	-
λ_{11}	-160	-	-53	-	-27	-	-18	-
λ_{12}	-10	-	-10	-	-10	-	-10	-
λ_{13}	-8	-	-8	-	-8	-	-8	-
λ_{14}	-10	-	-10	-	-10	-	-10	-
λ_{15}	-27	-	-27	-	-27	-	-27	-

Table 3. Eigenvalues of the DFIG for changing the proportional coefficient value K_{p3}

	σ $K_{p3} = 0.75$	ω	σ $K_{p3} = 1$	ω	σ $K_{p3} = 1.25$	ω	σ $K_{p3} = 1.5$	ω
λ_1	-10	-	-10	-	-10	-	-10	-
λ_2	-1542.9	-	-1542.9	-	-1542.9	-	-1542.9	-
λ_3	-1	+j50	-1	+j50	-1	+j50	-1	+j50
λ_4	-1	-j50	-1	-j50	-1	-j50	-1	-j50
λ_5	-2	+j3	-2	+j3	-2	+j3	-2	+j3
λ_6	-2	-j3	-2	-j3	-2	-j3	-2	-j3
λ_7	-1444	-	-1444	-	-1444	-	-1444	-
λ_8	-100	-	-100	-	-100	-	-100	-
λ_9	-27	-	-27	-	-27	-	-27	-
λ_{10}	-293	-	-219	-	-175	-	-146	-
λ_{11}	-27	-	-27	-	-27	-	-27	-
λ_{12}	-10	-	-10	-	-10	-	-10	-
λ_{13}	-8	-	-8	-	-8	-	-8	-
λ_{14}	-10	-	-10	-	-10	-	-10	-
λ_{15}	-27	-	-27	-	-27	-	-27	-

Table 4. Eigenvalues of the DFIG for changing the proportional coefficient value K_{p4}

	σ $K_{p4} = 0.05$	ω	σ $K_{p4} = 0.15$	ω	σ $K_{p4} = 0.3$	ω	σ $K_{p4} = 0.45$	Ω
λ_1	-10	-	-10	-	-10	-	-10	-
λ_2	-1542.9	-	-1542.9	-	-1542.9	-	-1542.9	-
λ_3	-1	+j50	-1	+j50	-1	+j50	-1	+j50
λ_4	-1	-j50	-1	-j50	-1	-j50	-1	-j50
λ_5	-2	+j3	-2	+j3	-2	+j3	-2	+j3
λ_6	-2	-j3	-2	-j3	-2	-j3	-2	-j3
λ_7	-1444	-	-1444	-	-1444	-	-1444	-
λ_8	-100	-	-100	-	-100	-	-100	-
λ_9	-27	-	-27	-	-27	-	-27	-
λ_{10}	-175	-	-175	-	-175	-	-175	-
λ_{11}	-27	-	-27	-	-27	-	-27	-
λ_{12}	-10	-	-10	-	-10	-	-10	-
λ_{13}	-8	-	-8	-	-8	-	-8	-
λ_{14}	-10	-	-10	-	-10	-	-10	-
λ_{15}	-160	-	-53	-	-27	-	-18	-

Table 5. Eigenvalues of the DFIG for changing the proportional coefficient value K_{p5}

	σ $K_{p5} = 5$	ω	σ $K_{p5} = 7.5$	ω	σ $K_{p5} = 10$	ω	σ $K_{p5} = 12.5$	Ω
λ_1	-10	-	-10	-	-10	-	-10	-
λ_2	-1542.9	-	-1542.9	-	-1542.9	-	-1542.9	-
λ_3	-1	+j50	-1	+j50	-1	+j50	-1	+j50
λ_4	-1	-j50	-1	-j50	-1	-j50	-1	-j50
λ_5	-2	+j3	-2	+j3	-2	+j3	-2	+j3
λ_6	-2	-j3	-2	-j3	-2	-j3	-2	-j3
λ_7	-1444	-	-1444	-	-1444	-	-1444	-
λ_8	-100	-	-100	-	-100	-	-100	-
λ_9	-27	-	-27	-	-27	-	-27	-
λ_{10}	-175	-	-175	-	-175	-	-175	-
λ_{11}	-27	-	-27	-	-27	-	-27	-
λ_{12}	-20	-	-13	-	-10	-	-8	-
λ_{13}	-8	-	-8	-	-8	-	-8	-
λ_{14}	-20	-	-13	-	-10	-	-8	-
λ_{15}	-27	-	-27	-	-27	-	-27	-

Table 6. Eigenvalues of the DFIG for changing the proportional coefficient value K_{p6}

	σ $K_{p6} = 5$	ω	σ $K_{p6} = 10$	ω	σ $K_{p6} = 15$	ω	σ $K_{p6} = 20$	ω
λ_1	-10	-	-10	-	-10	-	-10	-
λ_2	-1542.9	-	-1542.9	-	-1542.9	-	-1542.9	-
λ_3	-1	+j50	-1	+j50	-1	+j50	-1	+j50
λ_4	-1	-j50	-1	-j50	-1	-j50	-1	-j50
λ_5	-2	+j3	-2	+j3	-2	+j3	-2	+j3
λ_6	-2	-j3	-2	-j3	-2	-j3	-2	-j3
λ_7	-1444	-	-1444	-	-1444	-	-1444	-
λ_8	-100	-	-100	-	-100	-	-100	-
λ_9	-27	-	-27	-	-27	-	-27	-
λ_{10}	-175	-	-175	-	-175	-	-175	-
λ_{11}	-27	-	-27	-	-27	-	-27	-
λ_{12}	-10	-	-10	-	-10	-	-10	-
λ_{13}	-24	-	-12	-	-8	-	-6	-
λ_{14}	-10	-	-10	-	-10	-	-10	-
λ_{15}	-27	-	-27	-	-27	-	-27	-

Table 7. Eigenvalues of the DFIG for changing the integral coefficient value K_{i1}

	σ $K_{i1} = 50$	ω	σ $K_{i1} = 75$	ω	σ $K_{i1} = 100$	ω	σ $K_{i1} = 125$	ω
λ_1	-10	-	-10	-	-10	-	-10	-
λ_2	-1542.9	-	-1542.9	-	-1542.9	-	-1542.9	-
λ_3	-1	+j50	-1	+j50	-1	+j50	-1	+j50
λ_4	-1	-j50	-1	-j50	-1	-j50	-1	-j50
λ_5	-2	+j3	-2	+j3	-2	+j3	-2	+j3
λ_6	-2	-j3	-2	-j3	-2	-j3	-2	-j3
λ_7	-1444	-	-1444	-	-1444	-	-1444	-
λ_8	-50	-	-75	-	-100	-	-125	-
λ_9	-27	-	-27	-	-27	-	-27	-
λ_{10}	-175	-	-175	-	-175	-	-175	-
λ_{11}	-27	-	-27	-	-27	-	-27	-
λ_{12}	-10	-	-10	-	-10	-	-10	-
λ_{13}	-8	-	-8	-	-8	-	-8	-
λ_{14}	-10	-	-10	-	-10	-	-10	-
λ_{15}	-27	-	-27	-	-27	-	-27	-

Table 8. Eigenvalues of the DFIG for changing the integral coefficient value K_{i2}

	σ $K_{i2} = 4$	ω	σ $K_{i2} = 6$	ω	σ $K_{i2} = 8$	ω	σ $K_{i2} = 10$	ω
λ_1	-10	-	-10	-	-10	-	-10	-
λ_2	-1542.9	-	-1542.9	-	-1542.9	-	-1542.9	-
λ_3	-1	+j50	-1	+j50	-1	+j50	-1	+j50
λ_4	-1	-j50	-1	-j50	-1	-j50	-1	-j50
λ_5	-2	+j3	-2	+j3	-2	+j3	-2	+j3
λ_6	-2	-j3	-2	-j3	-2	-j3	-2	-j3
λ_7	-1444	-	-1444	-	-1444	-	-1444	-
λ_8	-100	-	-100	-	-100	-	-100	-
λ_9	-13	-	-20	-	-27	-	-33	-
λ_{10}	-175	-	-175	-	-175	-	-175	-
λ_{11}	-27	-	-27	-	-27	-	-27	-
λ_{12}	-13	-	-20	-	-27	-	-33	-
λ_{13}	-8	-	-8	-	-8	-	-8	-
λ_{14}	-10	-	-10	-	-10	-	-10	-
λ_{15}	-27	-	-27	-	-27	-	-27	-

Table 9. Eigenvalues of the DFIG for changing the integral coefficient value K_{i3}

	σ $K_{i3} = 140$	ω	σ $K_{i3} = 180$	ω	σ $K_{i3} = 220$	ω	σ $K_{i3} = 260$	ω
λ_1	-10	-	-10	-	-10	-	-10	-
λ_2	-1542.9	-	-1542.9	-	-1542.9	-	-1542.9	-
λ_3	-1	+j50	-1	+j50	-1	+j50	-1	+j50
λ_4	-1	-j50	-1	-j50	-1	-j50	-1	-j50
λ_5	-2	+j3	-2	+j3	-2	+j3	-2	+j3
λ_6	-2	-j3	-2	-j3	-2	-j3	-2	-j3
λ_7	-1444	-	-1444	-	-1444	-	-1444	-
λ_8	-100	-	-100	-	-100	-	-100	-
λ_9	-27	-	-27	-	-27	-	-27	-
λ_{10}	-112	-	-144	-	-176	-	-208	-
λ_{11}	-27	-	-27	-	-27	-	-27	-
λ_{12}	-10	-	-10	-	-10	-	-10	-
λ_{13}	-8	-	-8	-	-8	-	-8	-
λ_{14}	-10	-	-10	-	-10	-	-10	-
λ_{15}	-27	-	-27	-	-27	-	-27	-

Table 10. Eigenvalues of the DFIG for changing the integral coefficient value K_{i4}

	σ $K_{i4}= 4$	ω	σ $K_{i4}= 6$	ω	σ $K_{i4}= 8$	ω	σ $K_{i4}= 10$	ω
λ_1	-10	-	-10	-	-10	-	-10	-
λ_2	-1542.9	-	-1542.9	-	-1542.9	-	-1542.9	-
λ_3	-1	+j50	-1	+j50	-1	+j50	-1	+j50
λ_4	-1	-j50	-1	-j50	-1	-j50	-1	-j50
λ_5	-2	+j3	-2	+j3	-2	+j3	-2	+j3
λ_6	-2	-j3	-2	-j3	-2	-j3	-2	-j3
λ_7	-1444	-	-1444	-	-1444	-	-1444	-
λ_8	-100	-	-100	-	-100	-	-100	-
λ_9	-27	-	-27	-	-27	-	-27	-
λ_{10}	-175	-	-175	-	-175	-	-175	-
λ_{11}	-13	-	-20	-	-27	-	-33	-
λ_{12}	-10	-	-10	-	-10	-	-10	-
λ_{13}	-8	-	-8	-	-8	-	-8	-
λ_{14}	-10	-	-10	-	-10	-	-10	-
λ_{15}	-27	-	-27	-	-27	-	-27	-

Table 11. Eigenvalues of the DFIG for changing the integral coefficient value K_{i5}

	σ $K_{i5}= 50$	ω	σ $K_{i5}= 75$	ω	σ $K_{i5}= 100$	ω	σ $K_{i5}= 125$	ω
λ_1	-10	-	-10	-	-10	-	-10	-
λ_2	-1542.9	-	-1542.9	-	-1542.9	-	-1542.9	-
λ_3	-1	+j50	-1	+j50	-1	+j50	-1	+j50
λ_4	-1	-j50	-1	-j50	-1	-j50	-1	-j50
λ_5	-2	+j3	-2	+j3	-2	+j3	-2	+j3
λ_6	-2	-j3	-2	-j3	-2	-j3	-2	-j3
λ_7	-1444	-	-1444	-	-1444	-	-1444	-
λ_8	-100	-	-100	-	-100	-	-100	-
λ_9	-27	-	-27	-	-27	-	-27	-
λ_{10}	-175	-	-175	-	-175	-	-175	-
λ_{11}	-27	-	-27	-	-27	-	-27	-
λ_{12}	-5	-	-7	-	-10	-	-13	-
λ_{13}	-8	-	-8	-	-8	-	-8	-
λ_{14}	-5	-	-7	-	-10	-	-13	-
λ_{15}	-27	-	-27	-	-27	-	-27	-

Table 12. Eigenvalues of the DFIG for changing the integral coefficient value K_{i6}

	σ $K_{i6}= 80$	ω	σ $K_{i6}=100$	ω	σ $K_{i6}= 120$	ω	σ $K_{i6}= 140$	ω
λ_1	-10	-	-10	-	-10	-	-10	-
λ_2	-1542.9	-	-1542.9	-	-1542.9	-	-1542.9	-
λ_3	-1	+j50	-1	+j50	-1	+j50	-1	+j50
λ_4	-1	-j50	-1	-j50	-1	-j50	-1	-j50
λ_5	-2	+j3	-2	+j3	-2	+j3	-2	+j3
λ_6	-2	-j3	-2	-j3	-2	-j3	-2	-j3
λ_7	-1444	-	-1444	-	-1444	-	-1444	-
λ_8	-100	-	-100	-	-100	-	-100	-
λ_9	-27	-	-27	-	-27	-	-27	-
λ_{10}	-175	-	-175	-	-175	-	-175	-
λ_{11}	-27	-	-27	-	-27	-	-27	-
λ_{12}	-10	-	-10	-	-10	-	-10	-
λ_{13}	-5	-	-7	-	-8	-	-9	-
λ_{14}	-10	-	-10	-	-10	-	-10	-
λ_{15}	-27	-	-27	-	-27	-	-27	-

Table 13. The preferred range of values for the controllers coefficients for DFIG for the stability of the system.

Proportional Controllers Coefficients Range			Integral Controllers Coefficients Range		
Coefficient	Max	Min	Coefficient	Max	Min
K_{p1}	200	0.002	K_{i1}	99999	0.5
K_{p2}	16	0.00009	K_{i2}	29999	0.2
K_{p3}	438	0.003	K_{i3}	12499999	0.7
K_{p4}	17	0.0009	K_{i4}	299999	0.2
K_{p5}	200	0.009	K_{i5}	999999	5
K_{p6}	240	0.009	K_{i6}	1499999	8

7. Effect of Changing the Generator Parameters on the Stability

As the value of the resistance or inductance changes the stability degree will change. In this section we will try to find the relation between the increasing or decreasing these

values and the stability degree. Table (14) shows different values of the resistance and the corresponding eigenvalues. Figure (5) shows the relation between different values of the rotor resistance and the eigenvalues of the changed. From Figures (5) we conclude that as the resistance value of the rotor increase, the stability degree will increase.

Table 14. Eigenvalues of DFIG for different values of resistance.

	σ	ω	σ	ω	σ	ω	σ	ω
	Rr = 0.5		Rr = 0.05		Rr = 0.01		Rr = 0.005	
λ_1	-10	-	-10	-	-10	-	-10	-
λ_2	-1542.9	-	-1542.9	-	-1542.9	-	-1542.9	-
λ_3	-19	+j50	-10	+j50	-5	+j50	-1	+j50
λ_4	-1	-j50	-10	-j50	-5	-j50	-1	-j50
λ_5	-2	+j3	-2	+j3	-2	+j3	-2	+j3
λ_6	-2	-j3	-2	-j3	-2	-j3	-2	-j3
λ_7	-3578	-	-2911	-	-2244	-	-1444	-
λ_8	-100	-	-100	-	-100	-	-100	-
λ_9	-27	-	-27	-	-27	-	-27	-
λ_{10}	-175	-	-175	-	-175	-	-175	-
λ_{11}	-27	-	-27	-	-27	-	-27	-
λ_{12}	-10	-	-10	-	-10	-	-10	-
λ_{13}	-8	-	-8	-	-8	-	-8	-
λ_{14}	-10	-	-10	-	-10	-	-10	-
λ_{15}	-27	-	-27	-	-27	-	-27	-

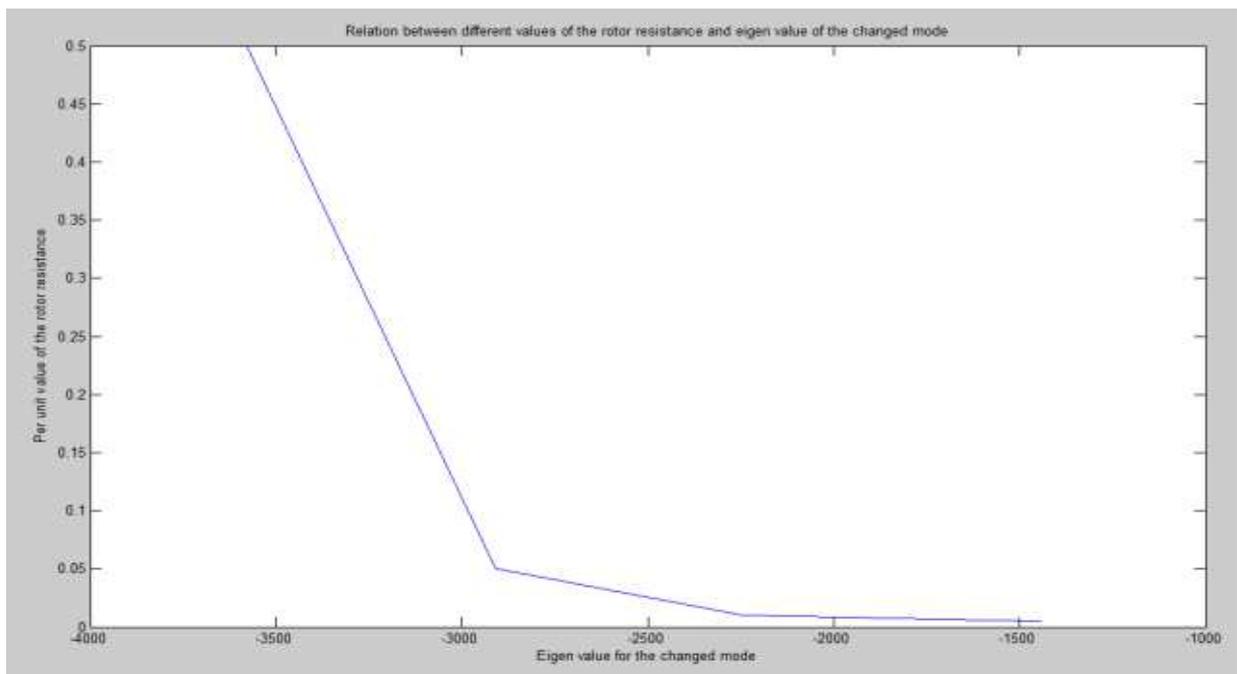


Figure 5. The relation between different values of the rotor resistance and the eigenvalues of the changed mode in case of DFIG.

Table 15. Eigenvalues of DFIG for different values of inductance.

	σ $L_s = 0.01$	ω	σ $L_s = 0.1$	Ω	σ $L_s = 1$	ω	σ $L_s = 2$	ω
λ_1	-10	-	-10	-	-10	-	-10	-
λ_2	-1542.9	-	-1542.9	-	-1542.9	-	-1542.9	-
λ_3	-1	+j50	-1	+j50	-1	+j50	-1	+j50
λ_4	-1	-j50	-1	-j50	-1	-j50	-1	-j50
λ_5	-2	+j3	-2	+j3	-2	+j3	-2	+j3
λ_6	-2	-j3	-2	-j3	-2	-j3	-2	-j3
λ_7	-1822	-	-1750	-	-1556	-	-1444	-
λ_8	-100	-	-100	-	-100	-	-100	-
λ_9	-27	-	-27	-	-27	-	-27	-
λ_{10}	-175	-	-175	-	-175	-	-175	-
λ_{11}	-27	-	-27	-	-27	-	-27	-
λ_{12}	-10	-	-10	-	-10	-	-10	-
λ_{13}	-8	-	-8	-	-8	-	-8	-
λ_{14}	-10	-	-10	-	-10	-	-10	-
λ_{15}	-27	-	-27	-	-27	-	-27	-

Table (15) shows different values of the inductance and the corresponding eigenvalues for DFIG. Figure (6) shows the relation between different values of the rotor inductance and the eigenvalues of the changed mode in case of DFIG. From Figures (9) we conclude that as the inductance value increase as the stability will decrease because of increasing the delay time.

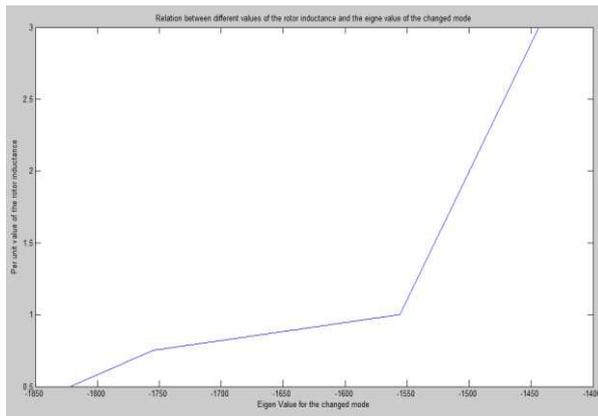


Figure 6. The relation between different values of the rotor inductance and the eigenvalues of the changed mode in case of DFIG.

8. Conclusion

The use of tidal currents as a renewable source of energy is very effective as it relies on the same technologies used in offshore wind generation and it is a more predictable source of energy. The overall dynamic system of the tidal current turbine for a single machine infinite bus system and the controllers used for improving the power system stability has been modeled. The equations for a small signal stability analysis for the generator has been formulated. Tidal current turbines without controllers do have the capability to sustain a small disturbance for a long period but it is more beneficial to use PI controllers with the tidal current turbines to improve system stability. As the value of the coefficients of the PI controllers change, the stability degree will change. For DFIG the most effective proportional coefficient controller is K_{p2} and the most effective

integral coefficient controller is K_{i3} . The preferred ranges of the controllers coefficients values for the system stability are concluded in this work. As the resistance value increases, the stability degree will increase but the system efficiency will decrease. On the contrary, as the inductance value of the machine increases, the stability degree will decrease. The future work will be focused on the optimal values for these coefficients to enhance the system stability.

Appendix

Tidal current turbine parameters

$R=18 \text{ m}$, $R_s=0.01 \text{ pu}$, $C_p=0.46$, $V_{tide}=4 \text{ m/s}$, $H_t=3 \text{ s}$, $H_g=0.5 \text{ s}$, $K_s=0.171$, $K_{pt}=10$, $K_{it}=100$, $K_s=10 \text{ pu}$, $D_s=3.14 \text{ pu}$.

Generator parameters

$L_m=2.9 \text{ pu}$, $L_r=0.156 \text{ pu}$, $L_s=0.171 \text{ pu}$, $R_r=0.005 \text{ pu}$.

Converter parameters

$V_{DC}=1.5 \text{ pu}$, $C=0.0001 \text{ pu}$.

Controller parameters

$K_{p1}=1 \text{ pu}$, $K_{p2}=0.3 \text{ pu}$, $K_{p3}=1.25 \text{ pu}$, $K_{p4}=0.3 \text{ pu}$, $K_{p5}=10 \text{ pu}$, $K_{p6}=15 \text{ pu}$, $K_{i1}=100 \text{ s}^{-1}$, $K_{i2}=8 \text{ s}^{-1}$, $K_{i3}=219 \text{ s}^{-1}$, $K_{i4}=8 \text{ s}^{-1}$, $K_{i5}=100 \text{ s}^{-1}$, $K_{i6}=120 \text{ s}^{-1}$.

Hamed H. H. Aly received the B.Sc. and M.Sc. degrees in electrical engineering with distinction, in 1999 and 2005, respectively, from Zagazig University, Egypt and the Ph.D. degree from Dalhousie University, Halifax, NS, Canada, in 2012. His research interests include Forecasting, Modeling, Control, power system quality, integration of the renewable energy into the electrical grid, Smart Grid and power system stability. Dr. Aly is currently doing his postdoctoral fellowship and working as an instructor at Dalhousie University in the Faculty of Engineering and the Faculty of Science.

M. E. El-Hawary (S'68–M'72–F'90) received the B.Eng. degree in electrical engineering with distinction from the University of Alexandria, Alexandria, Egypt, in

1968 and the Ph.D. degree from the University of Alberta, Edmonton, AB, Canada, in 1972. He was a Killam Memorial Fellow at the University of Alberta. He is now a Professor of electrical and computer engineering at Dalhousie University, Halifax, NS, Canada. He served on the faculty and was a Chair of the Electrical Engineering Department at Memorial University of Newfoundland for eight years. He was an Associate Professor of electrical engineering at the Federal University of Rio de Janeiro, Rio de Janeiro, Brazil, for two years and was an Instructor at the University of Alexandria. He pioneered many computational and artificial intelligence solutions to problems in economic/environmental operation of power systems. He has written ten textbooks and monographs and more than 122 refereed journal articles. He has consulted and taught for more than 42 years.

Dr. El-Hawary is a Fellow of the Engineering Institute of Canada (EIC) and the Canadian Academy of Engineering (CAE).

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