
Robust PID controller design for a modern type aircraft including handling quality evaluation

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To cite this article:

Mohammad Salem, Mohammad Ali Shahi Ashtiani. Robust PID Controller Design for a Modern Type Aircraft Including Handling Quality Evaluation. *American Journal of Aerospace Engineering*. Vol. 1, No. 1, 2014, pp. 1-7. doi: 10.11648/j.ajae.20140101.11

Abstract: In this paper we present classical PID controller approach in designing longitudinal Stability Augmentation System and pitch attitude control (SCAS) at nonlinear flight region for a high fidelity F-16 model including aerodynamic uncertainty. In high angle of attack, nonlinear effects of aerodynamic coefficients and atmospheric turbulence are the main challenge in designing and robustness of flight control system. A design scenario that combines deadbeat response and robust control (aerodynamic uncertainties and atmospheric turbulence) is presented. Simulation results show that the designed PI controller exhibits robustness property to system uncertainties.

Keywords: Aircraft Pitch Control, Deadbeat Controller, Robust Controller, Modern Type Aircraft

1. Introduction

Nowadays most modern fighter aircraft are designed statically relaxed stable or even unstable in certain modes to allow for extreme maneuverability as “in reference [1]”. Therefore, the stability and control characteristics of an aircraft may be estimated in the context of flying and handling qualities requirements. In the case that the aircraft fails to meet the requirements in some way, then it is necessary to consider remedial action. Quite often the imperfections occur simply as a result of the requirement for the aircraft to operate over an extended flight envelope and not necessarily as a result of an aerodynamic design oversight. Alternatively, this might be explained as the effects of aerodynamic non-linearity. The preferred solution is, therefore, to artificially modify, or augment, the apparent stability characteristics of the airframe as “in reference [2]”.

The flight control system (FCS) includes two feedback loops both of which derive their control signals from motion sensors appropriate to the requirements of the control laws. The outputs from the inner and outer loop controllers are summed and the resultant signal controls the aircraft. The inner loop control system alone comprises the SAS, it is usually the first part of the FCS to be designed and together with the airframe comprises the augmented aircraft. The outer loop provides the autopilot which enables the pilot to fly various maneuvers under automatic control. Autopilot control modes vary from the very simple, for example height

hold, pitch hold to the very complex, for example automatic landing as “in reference [2]”.

We know that development and testing of modern fighter aircraft partake a common emphasis on expanding their ability to fly at high angles of attack which mean that the aircraft is flown at angles near or beyond the wings maximum lift and into the post stall region where the lift versus alpha curve is nonlinear and subject to dynamic effects including separated flow as” in reference [3]”. Also angle of attack regions cannot be defined precisely, since the aircraft geometry and free stream conditions will create conditions as” in reference [4]”.

Many control systems are required to track an input demand. For example, an aircraft autopilot system ensures that an aircraft maintains a selected altitude. PID controllers are widely used, partly because they are effective and partly because they are straightforward to design. They are particularly common in systems that exhibit first- or second-order characteristics and for damped stable systems where PID control offers improvements in the system response as” in reference [5]”.

PID autopilots have been successfully integrated as real-time control and online navigation systems for aircraft. This is not only due to their simple structure and easy implementation, but also to their adequate performances. However, for successful implementation of such controllers, and without requiring complex mathematical development, parameter adjustment or tuning procedure is needed if

enhanced performance is to be achieved through the operating envelope. The tuning process, whereby the optimum values for the controller parameters are obtained, is a critical challenge.

Many studies were conducted to find the best way for tuning PID parameters in order to get adequate performances such as fast response, zero steady-state error, and minimum overshoot/undershoot. Even though there are only three parameters, PID parameter tuning is a difficult process because it must satisfying complex criteria within the limitations of system actuators. Also, the traditional PID controller only works for lower-order systems and lacks robustness against large system parameter uncertainties. This is due to the insufficient number of parameters to deal with the independent specifications of time-domain response such as settling time and overshooting as" in references [6,18,19]"

In this paper classic control approach (PI) is used to design SAS and pitch attitude at high angle of attack for a nonlinear, high fidelity F-16 model which satisfies the handling qualities requirements across the entire flight envelope of the model with aerodynamic uncertainties. It is assumed that the aerodynamic force and moment functions of the model are not known exactly and that they can change during flight due to unsteady aerodynamics at high angle of attack as" in reference [1]"

2. Aircraft Model Description

The aircraft model used in this work is that of the F-16 fighter aircraft with geometry and aerodynamic data as reported as "in reference [7]. The aerodynamic data in tabular form have been obtained from wind tunnel tests and valid for subsonic speed up to Mach number 0.6 for the range of angle of attack (α) and sideslip (β) as $-20^\circ \leq \alpha \leq 90^\circ$ and $-30^\circ \leq \beta \leq 30^\circ$. The wind tunnel tests were conducted on sufficiently close points to capture the nonlinear behavior of the aerodynamic force and moment coefficients.

Let $(V_T, \alpha, \theta, q) \in \mathbb{R}^4$ be the state vector where V_T is velocity, α is angle of attack, θ is the pitch angle, q is the pitch rate and $(F_T, \delta_e) \in \mathbb{R}^2$ be the control input vector where F_T is the engine thrust and δ_e the elevator angle. The nonlinear equations of motions of the aircraft longitudinal dynamic from as "in reference [8]" as follows:

$$\begin{aligned} \dot{V}_T &= \frac{1}{m}(-D + F_T \cos \alpha - mg \sin \gamma) \\ \dot{V}_T &= \frac{1}{m}(-D + F_T \cos \alpha - mg \sin \gamma) \\ \dot{\theta} &= q \\ \dot{q} &= \frac{1}{I_y}(M + F_T z_{TP}) \end{aligned} \quad (1)$$

Where m, I_y and γ are the mass, the inertia and the flight path angle and finally L, D and M are the aerodynamics

forces lift, drag and pitching moment, respectively.

3. Flight Control Design

The goal of this study is to design a SAS and pitch attitude to track pilot commands with responses that satisfy the handling qualities across the entire flight envelope of aircraft in presence of uncertain aerodynamic parameters.

For the design phase and dynamical analysis, the non-linear model is linearized for a given flight condition of interest. MATLAB LINMOD command generates the Jacobin matrices (A, B, C and D) for the state-space linear aircraft model from nonlinear F-16 aircraft model corresponding to the specified trim condition [9]. The linear models obtained in the trimming points used to design and analyze the controller are composed by following traditional set of linear equations:

$$\dot{x} = Ax + Bu \quad (2)$$

where the states are $x = (V_T, \alpha, q, \theta, \delta_e, F_T)$ and the control input $u = (\delta_e, F_T)$.

The actuator model $G_A(s)$ used for this work correspond a first order filter as "in reference [10]";

$$\frac{20.2}{s + 20.2} \quad (3)$$

At first, we design SAS where typically uses sensors to measure the body-axis angular rates of the vehicle, and feedback processed versions of these signals to servomechanisms that drive the aerodynamic control surfaces. SAS conventionally designed separately for the longitudinal and the lateral-directional dynamics and this is made possible by the decoupling of the aircraft dynamics in most flight conditions as "in reference [8]". The purpose of a pitch SAS is to provide satisfactory natural frequency and damping the short period. And if the frequency and damping are both unsatisfactory or the mode is unstable, usually an alpha feedback is necessary. "Fig.1" illustrates pitch axis stability with two feedbacks (q, α).

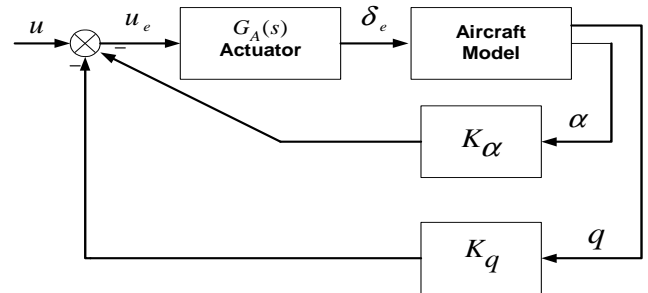


Figure 1. Pitch- axis stability augmentation.

Then, we design PI controller for pitch attitude and the block diagram of pitch attitude is shown in "Fig.2". Where $G_c(s)$ is the controller. The deadbeat response is defined as

having the following time domain performances:

1. Zero Steady-State Error (Zero-SSE).
2. Controllable settling time Ts.
3. Minimum rise time Tr90 (0-90% of the step height).

4. Percent Overshoot (P.O) and Percent Undershoot (P.U) less than 2%.

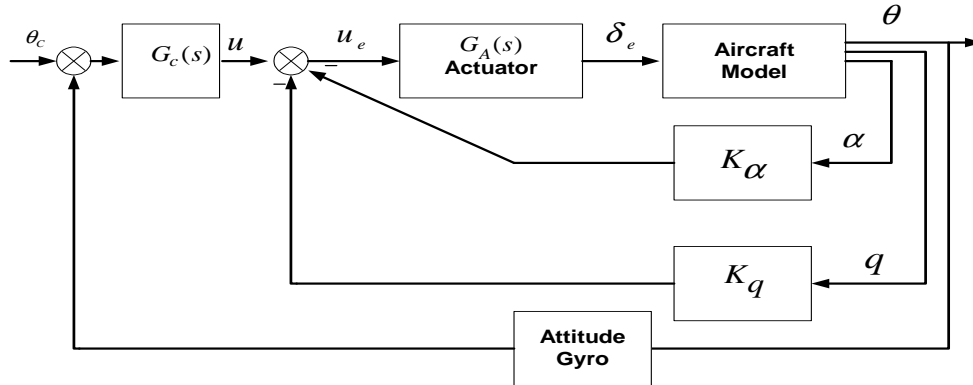


Figure 2. Pitch-attitude autopilot.

Fly at nonlinear flight region (high angle of attack); strongly depend to aerodynamic characteristics of aircraft. The designed controller should have an acceptable level of robustness to aerodynamic uncertainty. There are different aerodynamic derivatives in Longitudinal /

Lateral-Directional axis which have their influences in the equations of motion. It is shown that aerodynamic uncertainty data consist of increments or percentage variations in the important aerodynamic coefficients and derivatives as follow as “in references [11, 12]”:

$$C_{L_{\alpha}} (\pm 50\%); C_{m_{\alpha}} (\pm 10\%); C_{D_{\alpha}} (\pm 5\%) \text{ and } C_{L_q}, C_{m_q}, C_{D_q} (\pm 10\%) \quad (4)$$

4. Case Studies Simulations

This section presents the simulation results to design SAS and pitch hold using classical PI controller to the high-fidelity F-16 model at high angle of attack including aerodynamic uncertainties as “equation 4”. It is noted that simulation results are showed for linear (“equation 2”) and nonlinear model (“equation 1”) of aircraft at high angle of

attack. In this study, we make an investigation of robustness of designed controller in high angle of attack region for variation of speed between stall speed (V_{stall}) and minimum controllable speed (V_{min} ($1.05V_{stall}$)) and a mean speed ($(V_{stall} < V_{selected} < V_{min})$). Different case studies “Table . 1” are as follow:

Table 1. Design case studies.

Case	Altitude (ft)	Speed (ft/sec)	Trim Conditions	Gain SAS	Pitch	Handling Quality Levels
1- Without Uncertainties	Linear	Sea Level	$\alpha_{trim} = 20.012$ deg	$K_{\alpha} = 0.55$	$K_{\theta p} = 6.7$	Level I
	And nonlinear		$\delta_{e_{trim}} = 0.627$ deg	$K_q = 1.8$	$K_{\theta I} = 5.7$	
	Linear	5000	$\alpha_{trim} = 23.840$ deg	$K_{\alpha} = 0.8$	$K_{\theta p} = 12.9$	
	And nonlinear		$\delta_{e_{trim}} = 0.081$ deg	$K_q = 2.3$	$K_{\theta I} = 6.8$	
2- Including Aerodynamic Uncertainties	Linear	Sea Level	$\alpha_{trim} = 19.06$ deg	$K_{\alpha} = 0.56$	$K_{\theta p} = 6.95$	
	And nonlinear		$\delta_{e_{trim}} = 0.0989$ deg	$K_q = 2.0$	$K_{\theta I} = 6.15$	
	Linear	5000	$\alpha_{trim} = 22.59$ deg	$K_{\alpha} = 0.55$	$K_{\theta p} = 12.95$	
	And nonlinear		$\delta_{e_{trim}} = -0.1669$ deg	$K_q = 2.5$	$K_{\theta I} = 6.85$	
3- Effect of Measurement noise	Linear	Sea Level	$\alpha_{trim} = 20.012$ deg	$K_{\alpha} = 0.55$	$K_{\theta p} = 6.7$	Level I
	And nonlinear		$\delta_{e_{trim}} = 0.627$ deg	$K_q = 1.8$	$K_{\theta I} = 5.7$	
	Linear	5000	$\alpha_{trim} = 23.840$ deg	$K_{\alpha} = 0.8$	$K_{\theta p} = 12.9$	
	And nonlinear		$\delta_{e_{trim}} = 0.081$ deg	$K_q = 2.3$	$K_{\theta I} = 6.8$	
4- Effect of Atmospheric Turbulence	Linear	5000	$\alpha_{trim} = 23.840$ deg	$K_{\alpha} = 0.8$	$K_{\theta p} = 12.9$	
	And nonlinear		$\delta_{e_{trim}} = 0.081$ deg	$K_q = 2.3$	$K_{\theta I} = 6.8$	

4.1. Case 1

Investigation about effect of linear and nonlinear mathematical model to the designed controller. Simulation results are shown in “Fig 3”. As illustrated in “Fig 3”, type of modeling (linear / nonlinear), have the same time response.

4.2. Case 2

In this case, we make an investigation on time response of the designed SAS and pitch attitude controller in the presence of aerodynamics uncertainty. Simulation results are shown in “Fig.4”. As illustrated in “Fig.4”, the design SAS

and pitch attitude controller are robust with respect to aerodynamic uncertainty. Also, in “Fig.5”, effect of variation of altitude (from sea level to 30,000 ft.) and speed (from $V_{stall} < V_{selected} < V_{min}$ at each altitude) on variation of designed gain (e.g. gain scheduling) is presented.

4.3. Case 3

In this case, we make an investigation on time response of the designed SAS and pitch attitude controller to measurement noise and atmospheric turbulence. Measurement noise considers as an unstructured uncertainties where caused by imperfections in the sensors used to measure the output, and usually occurs at higher frequencies than the natural frequencies of the closed-loop system. To reduce the sensitivity of a closed-loop system to measurement noise (or to make the system robust with respect to measurement noise), the frequency response of the closed-loop system must have smaller gains at higher frequencies. Band-Limited White Noise” block for the measurement noise is used in simulation to study the effect of the noise on flight control system. In this paper is used “Noise power” parameter of the “Band-Limited White Noise” block to study this effect (i.e. we select value of 0.0001 for noise power as “in reference [13]”). “Fig.6” illustrates the results for these cases from noise power for linear and nonlinear model together. As indicated in “Fig.6”, the designed SAS and pitch attitude controller are robust with respect to noise.

4.4. Case 4

Finally, we make an investigation about effect of atmospheric turbulence on pitch hold, where atmospheric turbulence implementation are based on Dryden turbulence spectrum and handling qualities levels are defined from MIL_F_8785C as “in references[14 to 17,20]”. In this study Dryden turbulence is generated with the following parameters: flight altitude (H=5000 ft), velocity (V=195 ft/sec), and moderate intensity. “Fig. 7” illustrates the results for these cases from Dryden turbulence with moderate intensity for linear and nonlinear model together.

5. Conclusion and Discussion

In this paper, SAS and pitch attitude control for a modern type fighter has been developed based on classical PI techniques. It is demonstrated in numerical simulations that desirable handling qualities are achieved for high-fidelity F-16 model over a wide nonlinear flight region. Simulation results show that the designed SAS and controller are robust in time response with respect to aerodynamic uncertainties, measurement noise and atmospheric turbulence. Since the controller parameters are computed in advance and the tuning procedure is limited only to the cascade gain, the framework also provides an efficient and practical way for real-time PI parameter tuning.

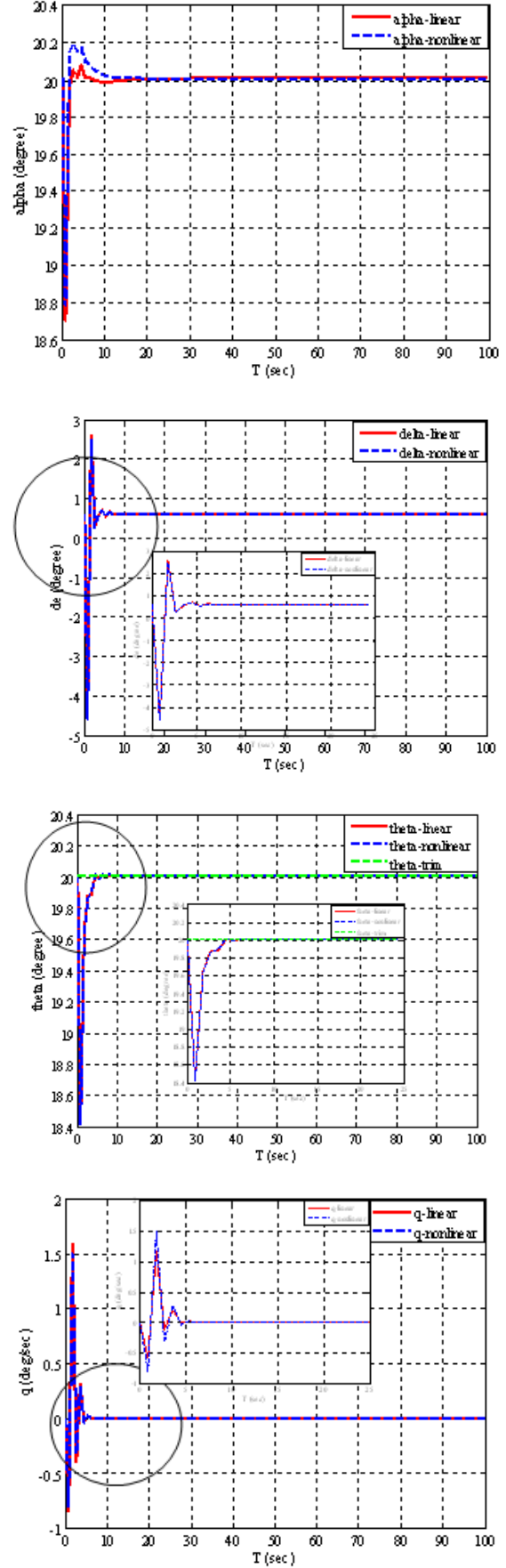


Figure 3. Aircraft responses for Case 1 (V=195 ft/sec ; H: Sea Level).

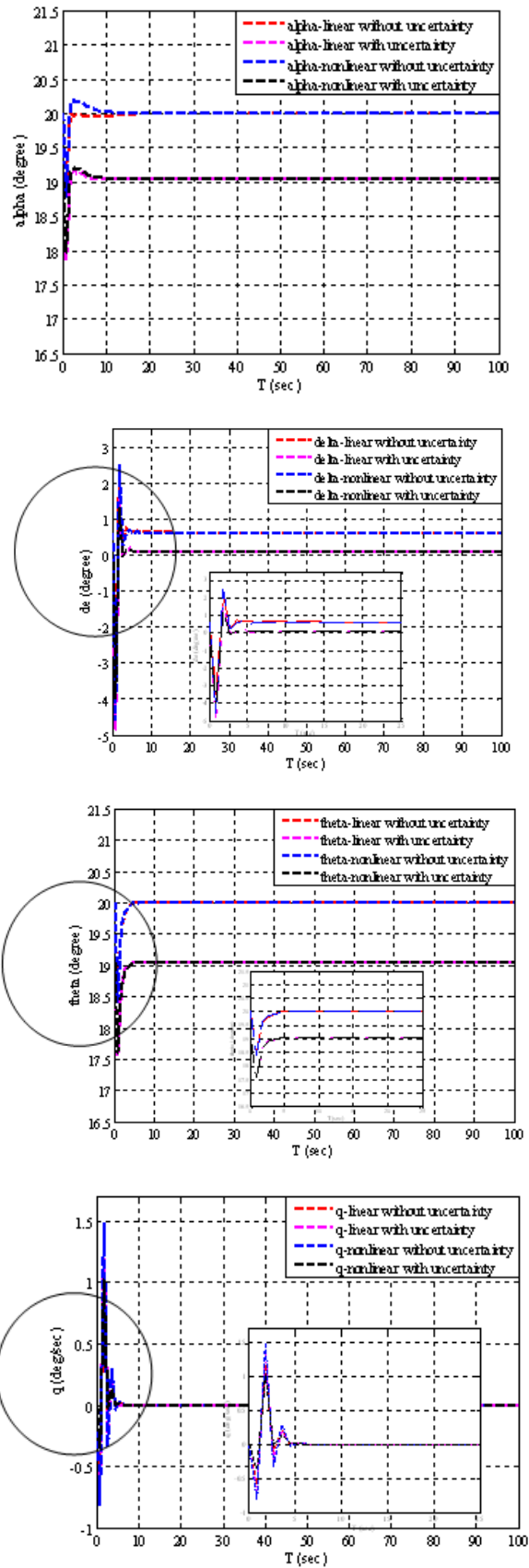


Figure 4. Aircraft responses at case 2 (V=195 ft/sec; H: Sea Level) including aerodynamic uncertainty.

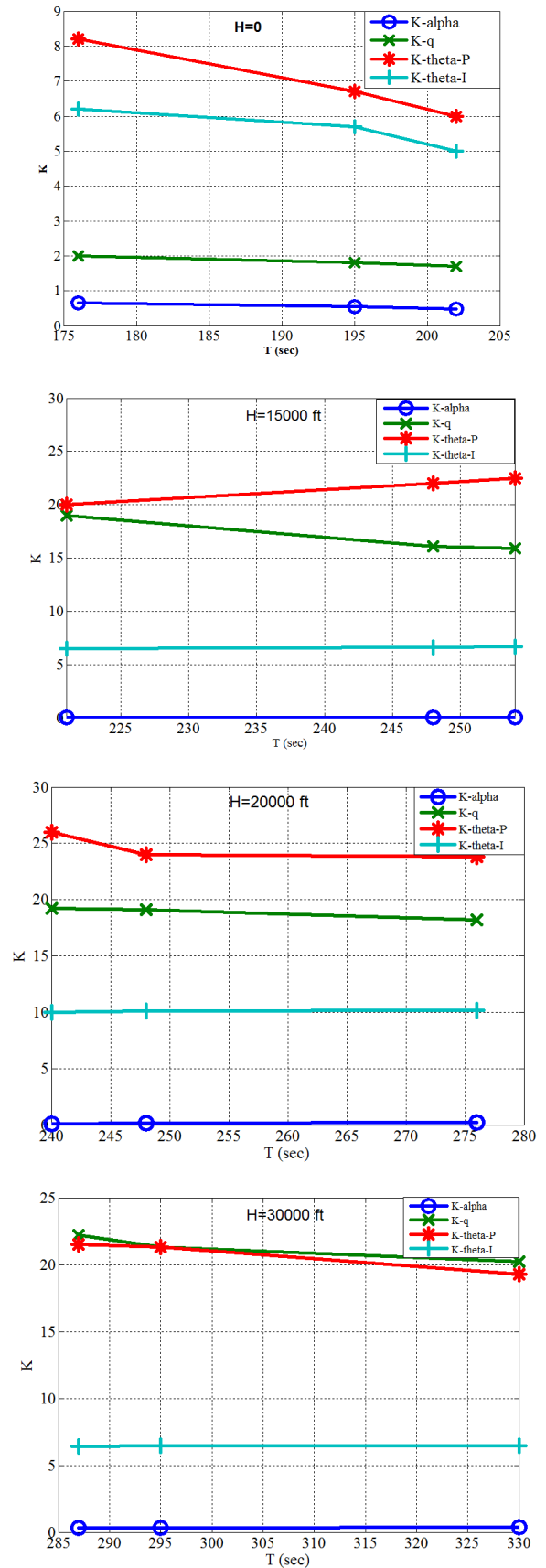


Figure 5. Gain scheduling as function of altitude and speed.

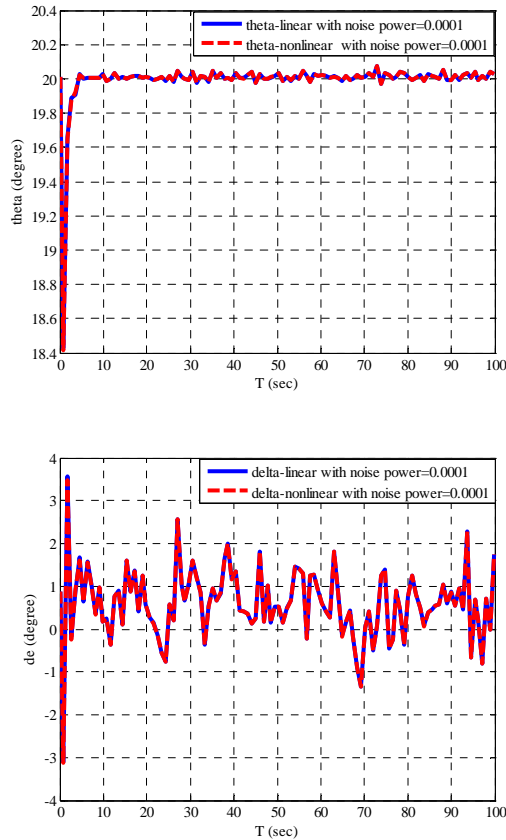


Figure 6. Aircraft responses to noise, case 3 ($V=195$ ft/sec; H : Sea Level).

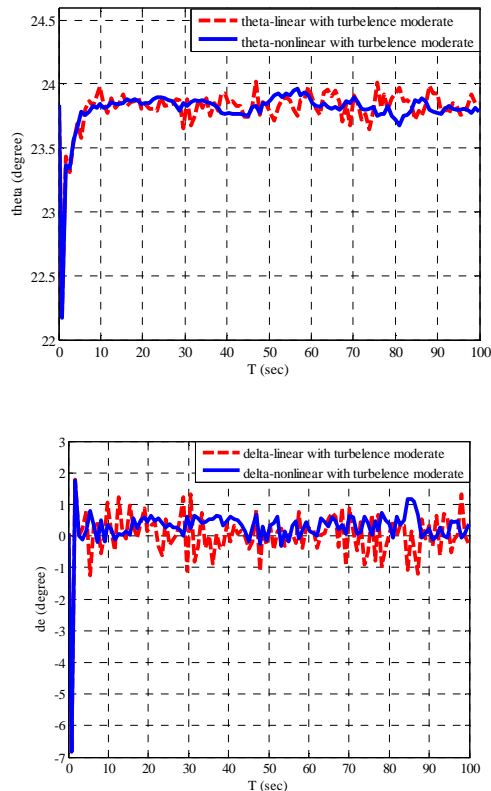


Figure 7. Aircraft responses at Case 4, with turbulence Dryden moderate model.

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